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Review text:

In the general framework of Quantum Mechanics of exactly solvable models (keeping the coordinates, for the sake of definiteness, real) our contemporary improvement of understanding of *complex* potentials leading to *real* (i.e., in principle, observable) energies proceeds in three steps. In the prehistory of the subject the first-step discoveries have been made of a close relationship between the reality of the spectrum and a Wick's rotation of the antisymmetric part of the potential. The second-step results are characteristic for the present stage of development. They are well exemplified in ref. [30] or by the Lévai's paper in question. People (cf. the list of references) calculate the pseudonorms of bound states in closed form. In particular, Lévai picks up the model with the name Rosen-Morse I and, in detail, he discusses some of the most important properties of the pseudonorms, e.g., their oscillatory excitation-dependence or their change after the backward Wick's rotation. All these efforts prepare the terrain for the final construction of the metric operator Θ . In this third-step activity the knowledge of the pseudonorms will prove vital, opening the way towards a climax of the story in the nearest future. Indeed, operator Θ will characterize physics and measurements. Equivalently, in the language of mathematics one can say that the specification of Θ will determine the Hamiltonian-assigned, non-standard operation of Hermitian conjugation in the correct though mathematically nontrivial physical Hilbert space of states.